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Significant thin shear layers in high Reynolds number turbulence

Takashi Ishihara, Gerrit E. Elsinga, & Julian C. R. Hunt



## Extreme events in real geophysical flows

August 8, 2017

Typhoon No. 5 in 2017



MODIS image captured by NASA's Aqua satellite



The longest lifetime: 456 hours

Typhoon track prediction

This case was difficult to predict.

13 models failed to predict <sup>各国の予想13パターン、意見割れる(7/31)</sup>



7月31日3時時点







Tornado in Toyohashi city Nine power poles toppled Injured people (caused by Typhoon No. 5)





Overturned trucks



豊橋市"竜巻"電柱9本倒れる ケガ人も

2017年8月7日 22:28

f シェアする

ツイートする

### 【台風5号上陸】あすは関東地方を通過か…今後の進路は?

要約

7日午後、愛知県豊橋市で、竜巻とみられる突風が発生し、トラックが横転するなどの 被害が出た。市内では子どもなど3人がけがをしている。

## Extreme events in real flow phenomena

- Extreme events in real flow phenomena are often caused by vortex motions
- Most of the real flow phenomena are high Reynolds number turbulence

Vortex motions in high Reynolds number turbulence may be the key to understand real flow phenomena such as those in geophysical flows

# Computational Science of turbulence

• Study of high–Reynolds number isotropic turbulence by direct numerical simulation, Ishihara, Gotoh, Kaneda, Ann. Rev. Fluid Mech. (2009)

#### DNS of turbulence with 4096<sup>3</sup> grid points on ES Kaneda et al (2003)



#### Figure 4

Snapshot of the intensity distributions of (a) the energy-dissipation rate  $\tilde{\epsilon} = \epsilon/(2\nu)$  and (b) the enstrophy  $\Omega = \omega^2/2$  on a cross section in DNS-ES at  $R_{\lambda} = 675$  in arbitrary units.



10λ 100η-



# Thin shear layers in turbulence

- Thin shear layers in high Reynolds number turbulence—DNS results, Ishihara, Kaneda, Hunt, Flow, Turbulence and Combustion, (2013)
- Thin shear layer structures in high Reynolds number turbulence, Hunt, I, Worth, Kaneda, Flow, Turbulence and Combustion, (2014)

Not observed in low Re



#### Sharp interface of high vorticity regions



**Fig. 3** Iso-surfaces of vorticity amplitude, showing vortices near the interface of the significant thin shear layer. Threshold values are set to  $|\omega| = \alpha (\omega^2)^{1/2}$ . **a**  $\alpha = 6$  (*pink*),  $\alpha = 2$  (*grey*); **b**  $\alpha = 6$  (*pink*),  $\alpha = 4$  (*grey*). In this graphics the brightness of the iso-surface is decreased due to the distance from view point, so that the far objects look dark. Also, the white color is used as the background color, so that directions (**b**) indicate that the visualized data (of finite size) do not have the iso-surfaces in that directions



# The scaling of straining motions in turbulence

 The scaling of straining motions in homogeneous isotropic turbulence, Elsinga, Ishihara, Goudar, Da Silva, Hunt, J. Fluid Mech. (2017)



### Re transitions in flow structure

Extreme dissipation is connected with strong shear at small scales and with large tangential velocity at large scales



# Extreme dissipation in high Re turbulence

• Extreme dissipation and intermittency in turbulence at very high Reynolds numbers, Elsinga, Ishihara, Hunt, Proceedings of the Royal Society A, (2020)

A model based on the DNS of turbulence which explains and predicts extreme dissipation in high Re turbulence



**Figure 2.** (*a*) Significant shear layer structure (blue) within a part of the flow domain ( $Re_{\lambda} > 150$ ). (*b*) Significant shear layer structure with sublayers in green ( $Re_{\lambda} > 1560$ ). (*c*) Significant shear layer structure with sub-sublayers in black ( $Re_{\lambda} > 1.8 \times 10^5$ ). For illustration purposes only, layers are not to scale. (Online version in colour.)

## In this talk

- DNSs of high Re turbulence
  - Energy spectrum and vortical structures
- Significant vortical structure in high Re turbulence – DNS results
  - Properties
  - Flow structure around the layer
  - Distribution
  - Time evolution and lifetime
- Significant layer in real geophysical flow
- Summary
- (Vortical structures in higher Re turbulence)

### Direct Numerical Simulations (DNSs) of turbulence

- Solve incompressible NS equations
  - No model, no numerical viscosity
- Resolve not only large scales but also small scales ( <>> LES)
- Simple geometry and simple forcing (negative viscosity)
- High accuracy, high resolution and high precision
  - e.g., Spectral method
    - To avoid extra uncertainties
- High performance (and many steps)
  - Reynolds number as high as possible

Computer resource is finite, We have to sacrifice some of these.

To explore Universality of Turbulence To understand the nature of high Re turbulence

### Reynolds Number & Development of Supercomputer



Scale ratio  $L/\eta \propto \operatorname{Re}^{3/4}$ Degree of Freedom  $(L/\eta)^3 \propto \operatorname{Re}^{9/4}$ Computational Cost  $\propto \operatorname{Re}^3$ 





## Energy Spectrum and Vortex Structures

• Low Re

 $Re < 10^{3}$ 

Inertial Range? Vortex Tubes!



• High Re

Re>104

Wide IR ! Vortex Clusters!









# Significant vortical structures in turbulence

Transition in the forms of the significant, high vorticity, intermittent structures:

from tube-like isolated vortices at  $R_{\lambda}$ <100

to complex thin-shear layers at  $R_{\lambda}$  >1000

### Significant, high vorticity, intermittent structure

Ishihara, Kaneda, Hunt FTAC (2013), Hunt, Ishihara, Worth, Kaneda FTAC (2014)



 $\cdots$  Complex thin-shear layers



Transition is consistent with quantitative results by Elsinga et al 2017

Width ~ O(L), Thickness ~ O( $\lambda) >> \eta$   $\cdots$  Isolated vortices

Length ~ O(L) Thickness ~ O(10 $\eta$ ) ~ O( $\lambda$ )

 $\lambda \sim L \operatorname{Re}^{-1/2}$ 



Thin Shear Layers in Homogeneous Isotropic Turbulence

### A slice of a strong layer-like cluster





### Thin Shear Layers in Homogeneous Isotropic Turbulence

(FTAC 2013, 2014)

High enstrophy, high dissipation

100

Averages over z in a certain range conditioned on the distance from the Right interface



Thickness ~ 4  $\lambda$ 











**Fig. 17** Distribution of the high  $|\omega_y|$  peaks (isolated regions) that satisfy  $|\omega_y| > \gamma \omega_{\text{Inside}}$ ; **a**  $\gamma = 2.0$ , **b**  $\gamma = 1.5$ . *Red circles* are for  $\omega_y > 0$  and *blue* ones are for  $\omega_y > 0$ . Circle size is determined as the area is proportional to the circulation intensity of each peak. The *right* and *left side arrows* represent the directions of  $\langle \mathbf{u} \rangle_{\text{Right}} - \langle \mathbf{u} \rangle_{\text{Inside}}$  and  $\langle \mathbf{u} \rangle_{\text{Left}} - \langle \mathbf{u} \rangle_{\text{Inside}}$  projected onto the *xz*-plane, respectively

### Thin Shear Layers in High Re Homogeneous Isotropic Turbulence



### Inside structure of the shear layers

Distribution of the strong vortices inside the layer

 $(\Delta = 2\pi/4096 \sim 3\eta$  : grid spacing)





 $\frac{\omega^{2}/2}{200} = \frac{2}{100} \frac{1}{200} \frac{1}{100} \frac{1}{10} \frac{1}{$ 

Thickness of the micro-scale vortices:  $\ell_v \sim 10\eta$  (insensitive to their strength)

Very strong vorticity of  $O(u_o/10 \eta)$   $>> u_{Kol} / \eta = 1/\tau_{Kol}$  (K41) Velocity jump of  $O(u_o)$  over distances of  $O(10 \eta)$  $>> u_{Kol} \sim u_o \operatorname{Re}^{-1/4}$  (K41)

The layers may dominate the extreme point values of the statistical distributions of dissipation, velocity and vorticity fluctuations Strong vortices within strong layers (much stronger than K41)



## Thin shear layer & Energy transfer

 Let be the filtering operation to remove all the Fourier modes with wavenumbers higher than k, then

$$T(\mathbf{x},k)\equiv\sum_{ij}(\overline{u_iu_j}-ar{u}_iar{u_j})ar{S}_{ij}$$

is the energy transfer at x across the wave number k

(e.g. Domaradzki et al 1990, Cerutti & Meneveau 1998, Chen et al 2003, Aoyama et al 2005)



T>0 downscale (from large to small) ,T<0 upscale (from small to large)

# Energy transfer T(x, k) and energy dissipation $\varepsilon$ near the layer



# Histograms of velocity components normalized by rms



## Flow structure around the layer

Layers as edged of large-scale motions

### Velocity vector directions

Number density of velocity vector directions in 465







Uniform velocity zones

### Velocity vector directions

Number density of velocity vector directions in 465









**Flow directions** 

### Uniform velocity zones & high vorticity regions

Number density of velocity vector directions in 465





The high vorticity regions are in between two different velocity zones and form a shear layer














Journal of the Physical Society of Japan Vol. 69, No. 10, October, 2000, pp. 3466-3467

Double Spirals around a Tubular Vortex in Turbulence

Shigeo KIDA and Hideaki MIURA

decaying  $Re_{\lambda}$  is 106

c.f.

Lundgren (1982) Kawahara (2005) Horiuti & Fujisawa (2008) Horiuti & Ozawa (2011)



Fig. 1. Double spiral structure. Contours of (a) vorticity magnitude, (b) the axial component, (c) magnitude of the cross-axial component, and (d) energy-dissipation rate on a cross-section of a low-pressure vortex in isotropic turbulence. Darker shade implies larger values in (a), (c) and (d). Vorticity is pointed into (or out of) the paper in gray (or white) area in (b). Vorticity vectors at every grid point are shown by arrows in (c). The coordinates of the cross-section, e<sub>1</sub> and e<sub>2</sub>, are measured in the unit of the grid width Δx taken in the numerical simulation. The Kolmogorov length is 2.0Δx. The levels of contours are 0, ±10<sup>-2+n/4</sup> (n = 1 ~ 5) in (a)–(c), ±10<sup>-8+n/4</sup> (n = 2 ~ 8) in (d).

## Velocity & vorticity near the layer



 $\langle \mathbf{u} \rangle_{Inside} / u' = (-0.94, \ 1.07, \ -0.80),$  $\langle \mathbf{u} \rangle_{Left} / u' = (-0.39, \ 1.25, \ -1.32),$  $\langle \mathbf{u} \rangle_{Right} / u' = (-1.74, \ 0.77, \ 0.58),$  $\delta \mathbf{U} \equiv \langle \mathbf{u} \rangle_{Left} - \langle \mathbf{u} \rangle_{Right}$ =(1.35, 0.47, -1.90)u' $|\delta \mathbf{U}| \approx 2.4u'$  $\langle \boldsymbol{\omega} \rangle_{Inside} / \omega' = (-0.15, -0.54, -0.54),$  $\langle \boldsymbol{\omega} \rangle_{Left} / \omega' = (-0.07, -0.01, 0.06),$  $\langle \boldsymbol{\omega} \rangle_{Right} / \omega' = (-0.08, -0.16, -0.09),$ 

 $|\left< oldsymbol{\omega} \right>_{Inside}| = 0.78 \omega'$ 

Horiuti & Ozawa 2011

 $\Omega = (3/2)\omega^{\prime 2}$ 

FIG. 2. Schematics of three modes of vorticity vector alignment along the vortex tube and dual sheets. The gray arrows denote vorticity vectors. (a) Mode 1, (b) Mode 2, (c) Mode 3.

# Distribution of the vortical clusters







## Data handling



			5	Ω=2174	
ligh Enstrophy ranking					
RANKING(new)	nx	ny	nz	$\Omega$ box	
1	4	5	5	6127	
2	5	6	5	<u>5850</u>	
3	4	6	5	5828	
4	5	4	5	5639	
5	6	6	5	5360	
6	5	5	5	5091	
7	4	7	5	5036	
509	2	7	1	796	
510	3	8	8	746	
511	2	7	7	690	
512	2	7	8	623	





#### Top10 Enstrophy subdomains



## Time evolution and lifetime



(In the most active subdomain of the 4096<sup>3</sup> DNS)



## The most significant shear layer from $t = t_0$ to $t_0+10\tau$ (= $t_0+2.55\lambda/u_o$ )







Subdomain: 4,4,5 & 4,5,5 & 4,6,5 Contour value:  $8\langle\omega^2\rangle^{0.5}$ Colour of arrows: v Slice colour variable: v 4 5 time: 0

Time: 0.000000

#### The extreme points $(\omega > 20 \langle \omega^2 \rangle^{1/2})$ in the most active subdomain



Generation of Spikes of enstrophy













 $\langle \omega^2/2 \rangle_{32\Delta x} = \langle \omega^2/2 \rangle_{1.4\lambda} > 7\Omega$ 

t/tau=0



 $\langle \omega^2/2 \rangle_{32\Delta x} = \langle \omega^2/2 \rangle_{1.4\lambda} > 7\Omega$ 



800

t/tau=13.3

 $\langle \omega^2/2 \rangle_{32\Delta x} = \langle \omega^2/2 \rangle_{1.4\lambda} > 7\Omega$ 



1200

 $\langle \omega^2/2\rangle_{32\Delta x} = \langle \omega^2/2\rangle_{1.4\lambda} > 7\Omega$ 



 $\langle \omega^2/2 \rangle_{32\Delta x} = \langle \omega^2/2 \rangle_{1.4\lambda} > 7\Omega$ 

t/tau=26.7



 $\langle \omega^2/2\rangle_{32\Delta x} = \langle \omega^2/2\rangle_{1.4\lambda} > 7\Omega$ 



 $\langle \omega^2/2 \rangle_{32\Delta x} = \langle \omega^2/2 \rangle_{1.4\lambda} > 7\Omega$ 



 $\langle \omega^2/2 \rangle_{32\Delta x} = \langle \omega^2/2 \rangle_{1.4\lambda} > 7\Omega$ 

t/tau=60



 $\langle \omega^2/2 \rangle_{32\Delta x} = \langle \omega^2/2 \rangle_{1.4\lambda} > 7\Omega$ 

t/tau=80



t/tau=100

6000

 $\langle \omega^2/2 \rangle_{8\Delta x} > 7\Omega$ 

 $\langle \omega^2/2\rangle_{32\Delta x} = \langle \omega^2/2\rangle_{1.4\lambda} > 7\Omega$ 



 $\langle \omega^2/2\rangle_{32\Delta x} = \langle \omega^2/2\rangle_{1.4\lambda} > 7\Omega$ 

t/tau=120



 $\langle \omega^2/2\rangle_{32\Delta x} = \langle \omega^2/2\rangle_{1.4\lambda} > 7\Omega$ 



 $\langle \omega^2/2\rangle_{32\Delta x} = \langle \omega^2/2\rangle_{1.4\lambda} > 7\Omega$ 







 $\langle \omega^2/2 \rangle_{32\Delta x} = \langle \omega^2/2 \rangle_{1.4\lambda} > 7\Omega$ 

t/tau=0



 $\langle \omega^2/2 \rangle_{32\Delta x} = \langle \omega^2/2 \rangle_{1.4\lambda} > 7\Omega$ 

t/tau=20



2400

t/tau=40

 $\langle \omega^2/2 \rangle_{32\Delta x} = \langle \omega^2/2 \rangle_{1.4\lambda} > 7\Omega$ 



3600

t/tau=60

 $\langle \omega^2/2 \rangle_{32\Delta x} = \langle \omega^2/2 \rangle_{1.4\lambda} > 7\Omega$


 $\langle \omega^2/2 \rangle_{32\Delta x} = \langle \omega^2/2 \rangle_{1.4\lambda} > 7\Omega$ 

t/tau=80

4800





 $\langle \omega^2/2 \rangle_{32\Delta x} = \langle \omega^2/2 \rangle_{1.4\lambda} > 7\Omega$ 



 $\langle \omega^2/2\rangle_{32\Delta x} = \langle \omega^2/2\rangle_{1.4\lambda} > 7\Omega$ 



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# Significant layer in real geophysical flow

Layer structures associated with typhoon 5 in 2017

# Precipitation Typhoon No. 5 in 2017





























# AM 05:00











# AM 05:15







# AM 05:25







































## AM 06:15






































# Significant layer in real geophysical flow

Layer structures associated with typhoon 5 in 2017

# Similar structure



## Low pressure core + vortical layer(spiral arms)

# Meso-Scale Model (MSM)

### Japan Meteorological Agency



Domains and topography of JMA's NWP models

Purpose: Weather warnings/advisories, Very short-range forecasts of precipitation
Grid size and/or number of grids: 5 km/817 x 661
Vertical levels/Top: 76/21.8 km
Initial conditions for MSM (every three hours): Best archived data generated by ensemble-based
4-D variational data assimilation





## Precipitation



### Amplitude of Vertical velocity



Vapor



Horizontal velocity

Tornado in Toyohashi city Nine power poles toppled Injured people (caused by Typhoon No. 5)





Overturned trucks



豊橋市"竜巻"電柱9本倒れる ケガ人も

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## https://tenki.jp/past/2017/08/07/radar/5/



# Summary

- We studied vortex cluster structures by visualizing the DNS data of high Re turbulence
  - Thin shear layer studied in detail in FTAC 2013 accompanies a large-scale tube-like low-pressure core
  - The structure is similar to double spirals observed in low Re turbulence (Kida & Miura 2000)
    - The spiral arm in low Re is a vortex layer
    - The spiral arm in high Re is the thin shear layer (a layer-like vortex cluster)
  - The lifetime of the significant layer is less than T.
- In a real geophysical flow, we observed a layer structure similar to that observed in the DNS. Analysis of the MSM data shows the following
  - Observed spiral rainband accompanies a shear layer
  - Generation of the tornado in Toyohashi may relate to the shear layer